The Zakon Series on Mathematical Analysis

Basic Concepts of Mathematics

Mathematical Analysis I

Mathematical Analysis II

The Zakon Series on Mathematical Analysis

Mathematical Analysis

Volume I

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Contents*

Preface ix

About the Author xi

Chapter 1. Set Theory 1

1–3. Sets and Operations on Sets. Quantifiers . . . 1
Problems in Set Theory . . . 6

4–7. Relations. Mappings . . . 8
Problems on Relations and Mappings . . . 14

8. Sequences . . . 15

9. Some Theorems on Countable Sets . . . 18
Problems on Countable and Uncountable Sets . . . 21

Chapter 2. Real Numbers. Fields 23

1–4. Axioms and Basic Definitions . . . 23

5–6. Natural Numbers. Induction . . . 27
Problems on Natural Numbers and Induction . . . 32

7. Integers and Rationals . . . 34

8–9. Upper and Lower Bounds. Completeness . . . 36
Problems on Upper and Lower Bounds . . . 40

10. Some Consequences of the Completeness Axiom . . . 43

11–12. Powers With Arbitrary Real Exponents. Irrationals . . . 46
Problems on Roots, Powers, and Irrationals . . . 50

13. The Infinities. Upper and Lower Limits of Sequences . . . 53
Problems on Upper and Lower Limits of Sequences in E^* . . . 60

Chapter 3. Vector Spaces. Metric Spaces 63

1–3. The Euclidean n-space, E^n . . . 63
Problems on Vectors in E^n . . . 69

4–6. Lines and Planes in E^n . . . 71
Problems on Lines and Planes in E^n . . . 75

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