

The Zakon Series on Mathematical Analysis

Basic Concepts of Mathematics

Mathematical Analysis I

Mathematical Analysis II



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The Zakon Series on Mathematical Analysis

Mathematical Analysis

VOLUME II

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The Trillia Group



West Lafayette, IN

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Mathematical Analysis II

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* "Starred" sections may be omitted by beginners.

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